## The function map

$$
\begin{aligned}
& \text { suclist :: [Int] -> [Int] } \\
& \text { suclist [] } \quad=[] \\
& \text { suclist (x:xs) }=\text { suc } \mathrm{x} \text { : suclist xs }
\end{aligned}
$$

$$
\begin{aligned}
& \text { sqrtlist :: [Float] -> [Float] } \\
& \text { sqrtlist [] } \quad=[] \\
& \text { sqrtlist (x:xs) }=\text { sqrt } x \text { : sqrtlist xs }
\end{aligned}
$$

map :: (a -> b) -> [a] -> [b]

$$
\operatorname{map} g[]=[]
$$

$$
\operatorname{map} g(x: x s)=g x: m a p g x s
$$

```
suclist :: [Int] -> [Int] sqrtlist :: [Float] -> [Float]
suclist = map suc sqrtlist = map sqrt
```


## The function filter

```
dropEven :: [Int] -> [Int]
dropEven [] = []
dropEven (x:xs) | odd x = x : dropEven xs
                        | otherwise = dropEven xs
dropUpper :: [Char] -> [Char]
dropUpper [] = []
dropUpper (x:xs) | isLower x = x : dropUpper xs
| otherwise = dropUpper xs
filter :: (a -> Bool) -> [a] -> [a]
filter g [] = []
filter g (x:xs) | g x = x : filter g xs
```

dropEven :: [Int] -> [Int] dropUpper :: [Char] -> [Char]
dropEven $=$ filter odd
dropUpper = filter isLower

## The function fold

```
add :: (List Int) -> Int prod :: (List Int) -> Int
add Nil = 0 prod Nil = 1
add (Cons x xs) = plus x (add xs) prod (Cons x xs) = times x (prod xs)
concat :: List (List a) -> List a
concat Nil = Nil
concat (Cons x xs) = append x (concat xs)
fold :: (a -> b -> b) -> b -> (List a) -> b
fold g e Nil = e
fold g e (Cons x xs) = g x (fold g e xs)
add :: (List Int) -> Int prod :: (List Int) -> Int
add = fold plus 0 prod = fold times 1
```

```
concat :: List (List a) -> List a
```

concat :: List (List a) -> List a
concat = fold append Nil

```
concat = fold append Nil
```


## The function foldr

```
sum :: [Int] -> Int
prod :: [Int] -> Int
prod [] = 1
prod (x:xs) = x * prod xs
```

```
concat :: [[a]] -> [a]
```

concat :: [[a]] -> [a]
concat [] = []
concat [] = []
concat (x:xs) = x ++ concat xs
concat (x:xs) = x ++ concat xs
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr g e [] = e
foldr g e (x:xs) = g x (foldr g e xs)
V
sum :: [Int] -> Int
sum = foldr (+) 0

```
```

prod :: [Int] -> Int

```
prod :: [Int] -> Int
prod = foldr (*) 1
```

prod = foldr (*) 1

```
```

concat :: [[a]] -> [a]

```
concat :: [[a]] -> [a]
concat = foldr (++) []
```

concat = foldr (++) []

```
```

