

- \succ *Reduction Relation* iff \succ well founded, stable, and monotonic.
- \succ *Reduction Order* iff \succ well founded, stable, monotonic, and transitive.

Thm. 4.3.4

\mathcal{R} terminates iff

there exists a reduction relation \succ with $l \succ r$ for all $l \rightarrow r \in \mathcal{R}$.

Embedding Order: $s \succ_{emb} t$ iff

- $s = f(s_1, \dots, s_n)$ and $s_i \succeq_{emb} t$ for some $i \in \{1, \dots, n\}$ or
- $s = f(s_1, \dots, s_n)$, $t = f(t_1, \dots, t_n)$, $s_i \succ_{emb} t_i$ for some $i \in \{1, \dots, n\}$, and $s_j \succeq_{emb} t_j$ for all $j \in \{1, \dots, n\}$ with $j \neq i$.

$$\begin{array}{llll}
 \text{minus}(x, \mathcal{O}) & \rightarrow & x & \text{minus}(x, \mathcal{O}) \succ_{emb} x \\
 \text{minus}(\mathcal{O}, \text{succ}(y)) & \rightarrow & \mathcal{O} & \text{minus}(\mathcal{O}, \text{succ}(y)) \succ_{emb} \mathcal{O} \\
 \text{minus}(\text{succ}(x), \text{succ}(y)) & \rightarrow & \text{minus}(x, y) & \text{minus}(\text{succ}(x), \text{succ}(y)) \succ_{emb} \text{minus}(x, y)
 \end{array}$$