

# Automated Detection of Non-Termination and NullPointerExceptions for Java Bytecode

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# Automated Non-Termination Analysis

- Logic programs:  
De Schreye '90 ..., Payet & Mesnard '06, ...
- TRSs and SRSs:  
Giesl et. al '05, Payet '06, ...
- C:  
Gupta et. al '08, ...
- JBC:  
Velroyen '08, Payet & Spoto '09

- 1 Introduction
- 2 Termination Graphs
- 3 Witness generation
- 4 Looping Non-Termination
- 5 Conclusion

# The example

```
class Loop {  
  void main(String[] a){  
    int i = 0;  
    int j = a.length;  
    while (i < j) {  
      i += a[i].length();}}}
```

- 1 Adds up lengths.

# The example

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- 1 Adds up lengths.
- 2 May not terminate.

# The example

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class Loop {  
    void main(String[] a){  
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- 1 Adds up lengths.
- 2 May not terminate.
- 3 May throw NullPointerException

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main(String[] a):
00: iconst_0      #load 0 to stack
01: istore_1     #store to i
02: aload_0      #load a to stack
03: arraylength  #get array length
04: istore_2     #store to j
05: iload_1      #load i to stack
06: iload_2      #load j to stack
07: if_icmpge 22 #jump to end if i >= j
10: iload_1      #load i to stack
11: aload_0      #load a to stack
12: iload_1      #load i to stack
13: aaload       #load a[i]
14: invokevirtual length #call length()
17: iadd         #add length and i
18: istore_1     #store to i
19: goto 05
22: return

length():
00: aload_0      #load this to stack
01: getfield count #load count field
04: ireturn      #return it
```

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class Loop {
  void main(String[] a){
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    while (i < j) {
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```

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- 2 May not terminate.
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# Abstract JAVA virtual machine states

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```

00		a: $a_1$		$\varepsilon$
$a_1$ :String[]		$i_1$		$i_1: [\geq 0]$



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```

00		a: a <sub>1</sub>		ε
a <sub>1</sub> :String[]		i <sub>1</sub>		i <sub>1</sub> : [≥0]

stack frame:

# Abstract JAVA virtual machine states

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```

00	a: a <sub>1</sub>	ε
a <sub>1</sub> :String[]	i <sub>1</sub>	i <sub>1</sub> : [≥0]

## stack frame:

- Next program instruction

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00	a: a <sub>1</sub>	ε
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## stack frame:

- Next program instruction
- Local variables
- Operand stack

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00		a: a <sub>1</sub>		ε
a <sub>1</sub> : String[]		i <sub>1</sub>		i <sub>1</sub> : [≥0]

## stack frame:

- Next program instruction
- Local variables
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## heap information:

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00		a: $a_1$		$\varepsilon$
		$a_1: \text{String}[]$	$i_1$	$i_1: [\geq 0]$

## stack frame:

- Next program instruction
- Local variables
- Operand stack

## heap information:

- at  $a_1$  is String array  
content unknown, length is  $i_1$

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## stack frame:

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## stack frame:

- Next program instruction
- Local variables
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## heap information:

- at  $a_1$  is String array  
content unknown, length is  $i_1$
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- Known String object:  
 $\text{String}(\text{count} = i_3, \dots)$

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- at  $i_1$  is a non-negative integer
- Known String object:  
String(count =  $i_3, \dots$ )
- Unknown String object:  
String(?)



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Only explicit sharing

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00: aload_0  
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```

00   $a: a_1 \mid \epsilon$ $a_1: \text{String}[] \quad i_1 \quad i_1: [\geq 0]$	A
---	---

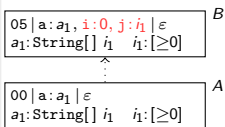
### State A:

- What can happen when evaluating main?
- $a_1$ : Unknown array of String objects
- $i_1$ :  $a_1$ 's unknown length

```

main(String[] a):
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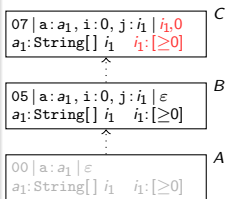
### State B:

- Stored 0 to i
- Stored arraylength  $i_1$  to j
- *Evaluations* from A to B

```

main(String[] a):
00: iconst_0
01: istore_1
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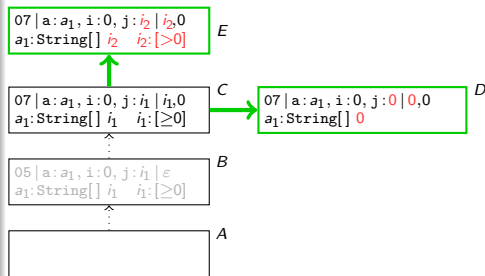
### State C:

- Load `i` (0) and `j` (`i1`) to operand stack
- `if_icmpge` cannot be evaluated

```

main(String[] a):
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03: arraylength
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```



State C, D, E:

- Load  $i$  (0) and  $j$  ( $i_1$ ) to operand stack
- `if_icmpge` cannot be evaluated yet:

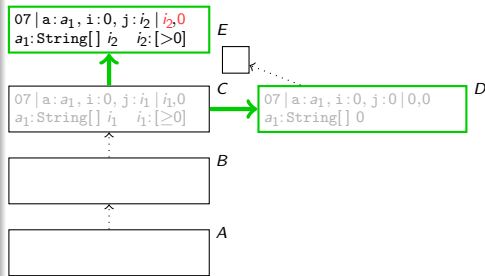
⇒ *Refine* information:

- In  $D$ , consider case  $i_1 = 0$
- In  $E$ , consider case  $i_1 > 0$

```

main(String[] a):
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03: arraylength
04: istore_2
05: iload_1
06: iload_2
07: if_icmpge 22
10: iload_1
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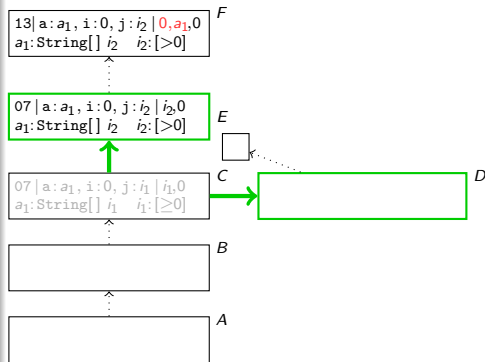
States D, E, F:

- D jumps to end of method

```

main(String[] a):
00: iconst_0
01: istore_1
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03: arraylength
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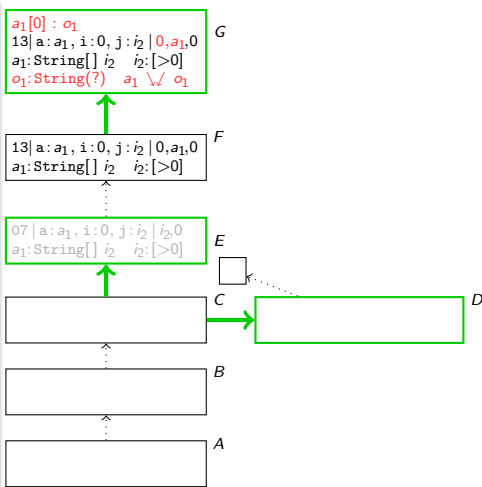
States *D, E, F*:

- *D* jumps to end of method
- *E* evaluates to *F*
- Loads array *a* (*a*<sub>1</sub>) and index *i* (0) to stack
- Cannot evaluate `aaLoad`: *a*<sub>1</sub>[0] not known

```

main(String[] a):
00: iconst_0
01: istore_1
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### State G:

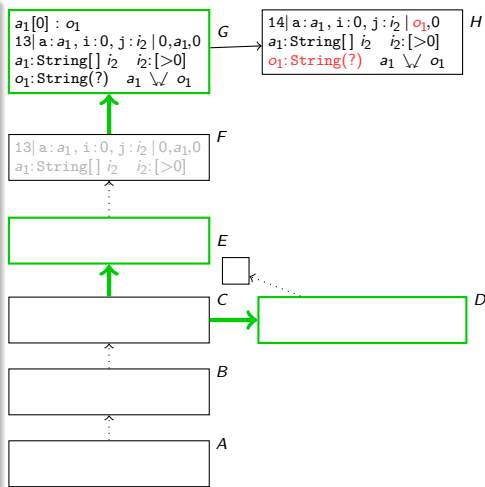
- *Refinement* of F
- $o_1$  created: null or unknown String
- $a_1 \vee o_1$ : They *share*
- $o_1$  is value at  $a_1[i_2]$



```

main(String[] a):
00: iconst_0
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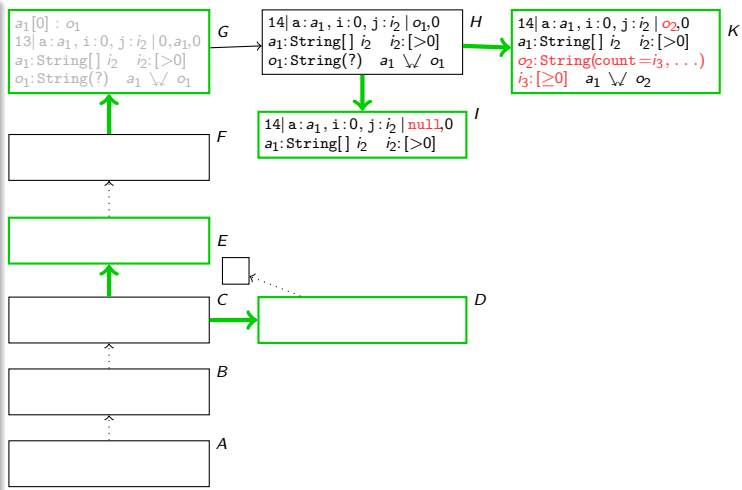
States H to K:

- H evaluated from G, loaded  $o_1$  to stack
- invoke may throw NullPointerException

```

main(String[] a):
00: iconst_0
01: istore_1
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**States H to K:**

- H evaluated from G, loaded  $o_1$  to stack
- invoke may throw `NullPointerException`

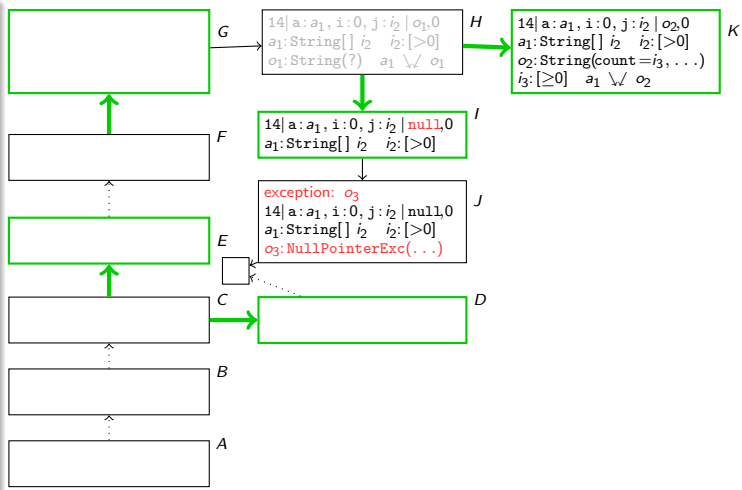
$\Rightarrow$  **Refinement:**

- I: Case  $o_1$  is null
- K: Case  $o_1$  is some object with fields

```

main(String[] a):
00: iconst_0
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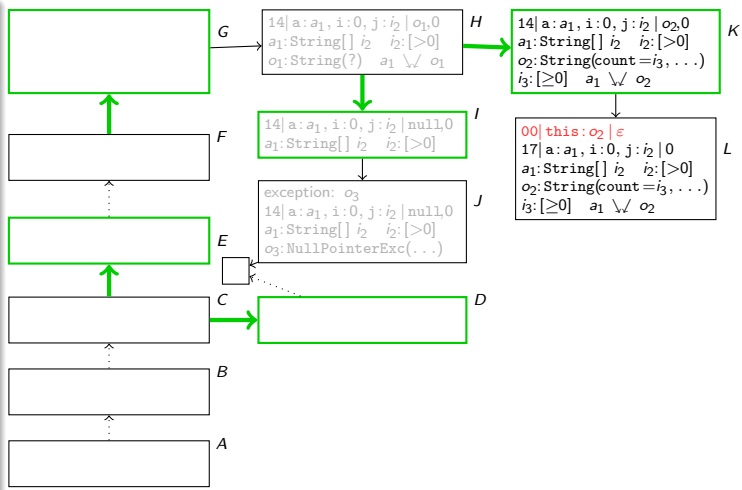
⇒ Refinement:

- I: Case  $o_1$  is null (leads to NPE)
- K: Case  $o_1$  is some object with fields

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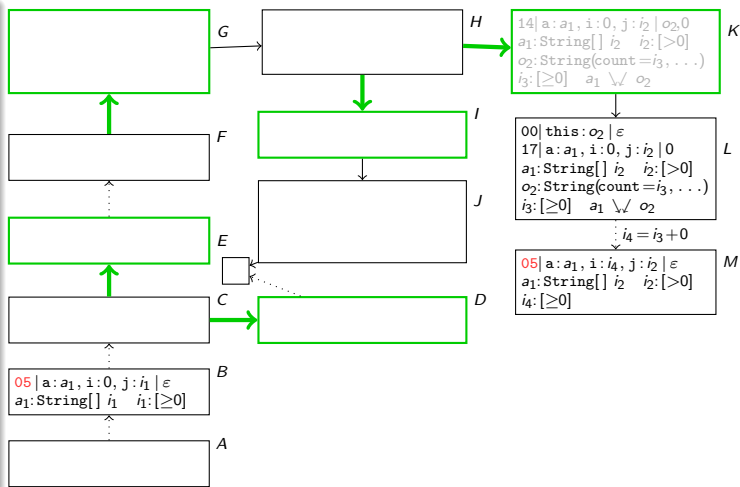
State L, M, N:

- Evaluation to L: New stack frame on top

```

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13: aaload
14: invoke length
17: iadd
18: istore_1
19: goto 05
22: return
length():
00: aload_0
01: getfield count
04: ireturn

```



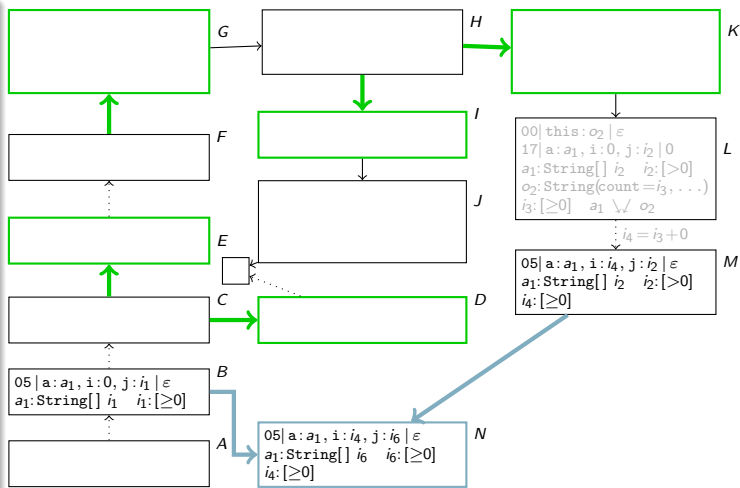
State L, M, N:

- Evaluation to L: New stack frame on top
- Evaluation to M: Retrieve length, add to i

```

main(String[] a):
00: iconst_0
01: istore_1
02: aload_0
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05: iload_1
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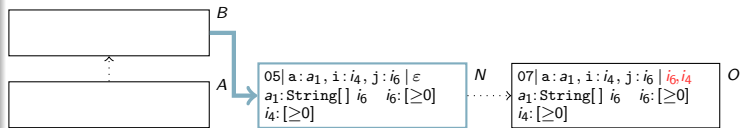
State L, M, N:

- Evaluation to L: New stack frame on top
- Evaluation to M: Retrieve length, add to i
- B and M similar: Merge states, get N
- N represents both B and M (*instances* of N)

```

main(String[] a):
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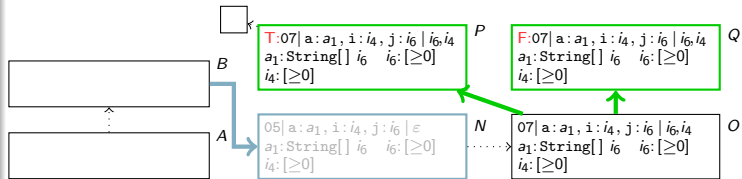
States  $O$  to  $S$ :

- Evaluate to  $O$ : Load  $i, j$  to stack

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States *O* to *S*:

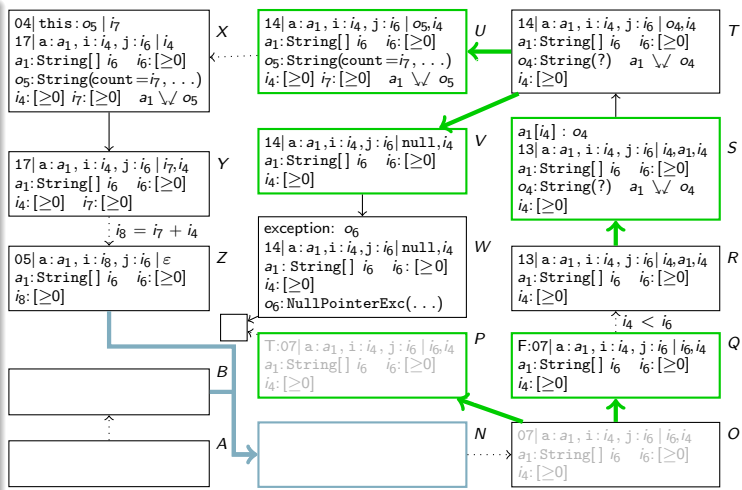
- Evaluate to *O*: Load *i*, *j* to stack
- Refine *O* to *P*, *Q*: Decide result of `if_icmpge`



```

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    length():
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```



**States O to S:**

- Evaluate to O: Load i, j to stack
- Refine O to P, Q: Decide result of if\_icmpge
- Rest as before



# Termination graph construction

- 1 Choose (abstract) start state

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  - 2 Perform
    - symbolic evaluation
    - information **refinement**
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- until all leaves are program ends

# Termination graph construction

- 1 Choose (abstract) start state
- 2 Perform
  - symbolic evaluation
  - information **refinement**
  - **instantiation** (may need to *merge* states)until all leaves are program ends
- 3 Recursion and modularity supported (cf. RTA'11)

- 1 Introduction
- 2 Termination Graphs
- 3 Witness generation**
- 4 Looping Non-Termination
- 5 Conclusion

- Termination graphs are *overapproximations* of all runs

# Witness generation

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- Let state  $e$  occur in graph starting in  $s$
- $e$  really occurring in runs from  $s$ ?



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## Definition

$w$  *witness* for  $e$   $\Leftrightarrow$  all runs from  $w$  lead to  $e$

# Witness generation

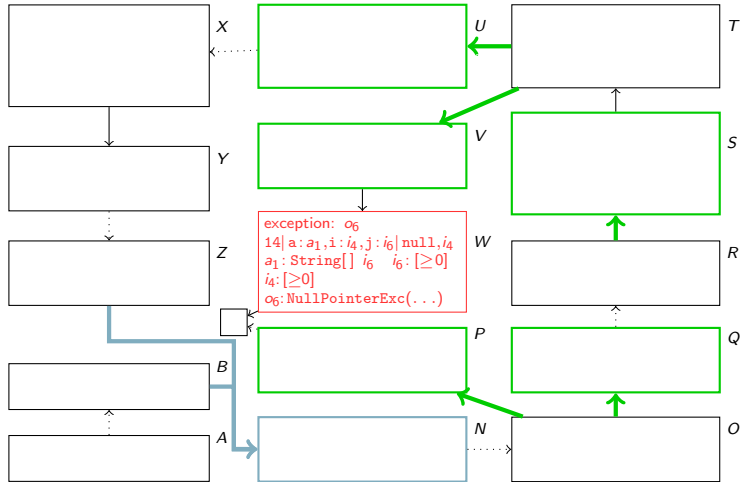
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$w$  *witness* for  $e \Leftrightarrow$  all runs from  $w$  lead to  $e$

Re-use graph: Traverse edges backwards

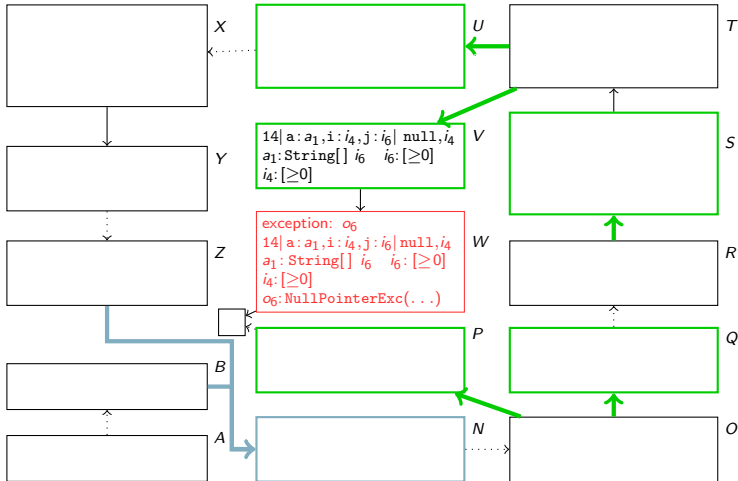


- $W$ : program ends with a `NullPointerException`

⇒ Find witness

### Witness for $W$

```
exception: o6  
14 | a: a1, i: i4, j: i6 | null, i4  
a1: String[] i6 i6: [≥0]  
i4: [≥0]  
o6: NullPointerException(...)
```



- $V$  evaluated to  $W$

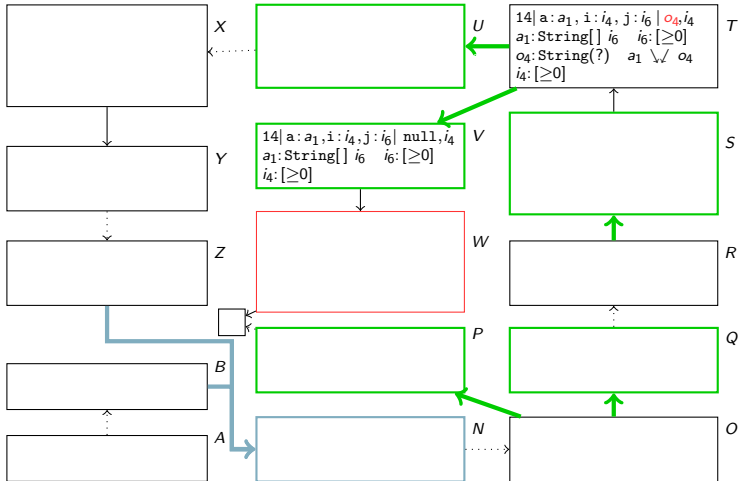


### Witness for $W$

exception:  $o_6$   
 $14 \mid a: a_1, i: i_4, j: i_6 \mid \text{null}, i_4$   
 $a_1: \text{String}[] \quad i_6 \quad i_6: [\geq 0]$   
 $i_4: [\geq 0]$   
 $o_6: \text{NullPointerException}(\dots)$

$14 \mid a: a_1, i: i_4, j: i_6 \mid \text{null}, i_4$   
 $a_1: \text{String}[] \quad i_6 \quad i_6: [\geq 0]$   
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 $i_4: [\geq 0]$



- $V$  evaluated to  $W$

⇒ Reverse evaluation step

- $T$  refined to  $V$

⇒ Re-use current witness





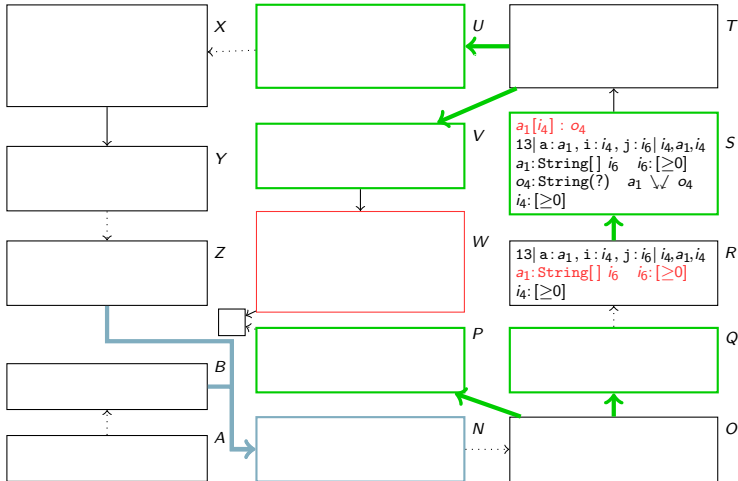
### Witness for $W$

exception:  $o_6$   
 14 |  $a: a_1, i: i_4, j: i_6$  | null,  $i_4$   
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 $i_4: [\geq 0]$

$a_1[i_4]: \text{null}$   
 13 |  $a: a_1, i: i_4, j: i_6$  |  $i_4, a_1, i_4$   
 $a_1: \text{String}[]$   $i_6$   $i_6: [\geq 0]$   
 $i_4: [\geq 0]$



- $R$  refined to  $S$ : Re-use current witness

## Witness for $W$

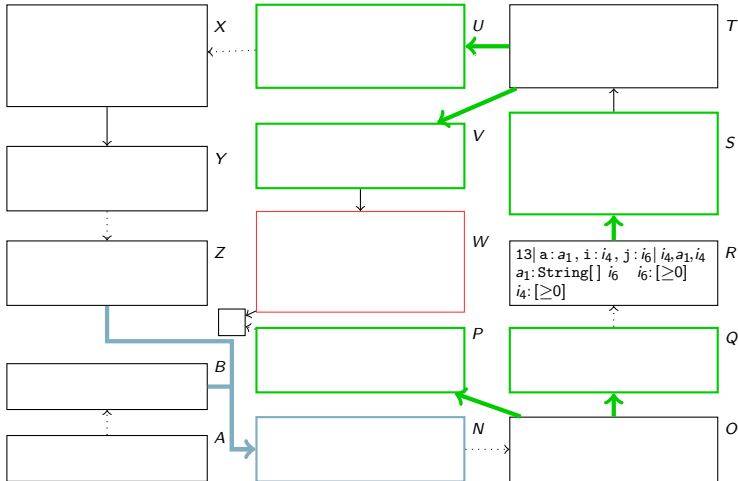
exception:  $o_6$   
 14 |  $a: a_1, i: i_4, j: i_6$  | null,  $i_4$   
 $a_1: \text{String}[]$   $i_6$   $i_6: [\geq 0]$   
 $i_4: [\geq 0]$   
 $o_6: \text{NullPointerException}(\dots)$

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 $a_1: \text{String}[]$   $i_6$   $i_6: [\geq 0]$   
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 $a_1: \text{String}[]$   $i_6$   $i_6: [\geq 0]$   
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$a_1[i_4]: \text{null}$   
 13 |  $a: a_1, i: i_4, j: i_6$  |  $i_4, a_1, i_4$   
 $a_1: \text{String}[]$   $i_6$   $i_6: [\geq 0]$   
 $i_4: [\geq 0]$

13 |  $a: a_2, i: 0, j: 1$  |  $Q, a_2, 0$   
 $a_2: \text{String}[]$  {null}



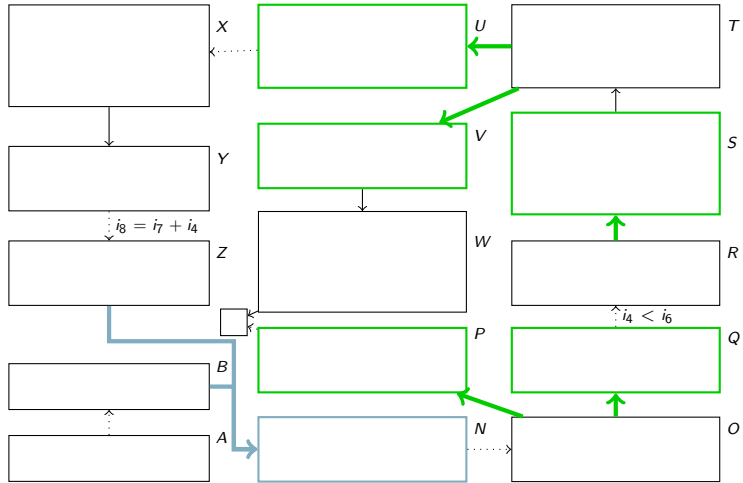
- $R$  refined to  $S$ : Re-use current witness - **No!**

- $a_1$  too abstract to keep information

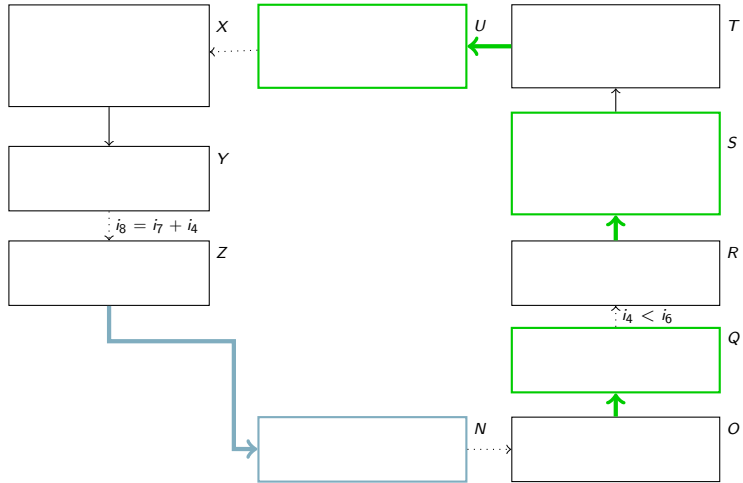
⇒ Instantiate array and index by concrete values



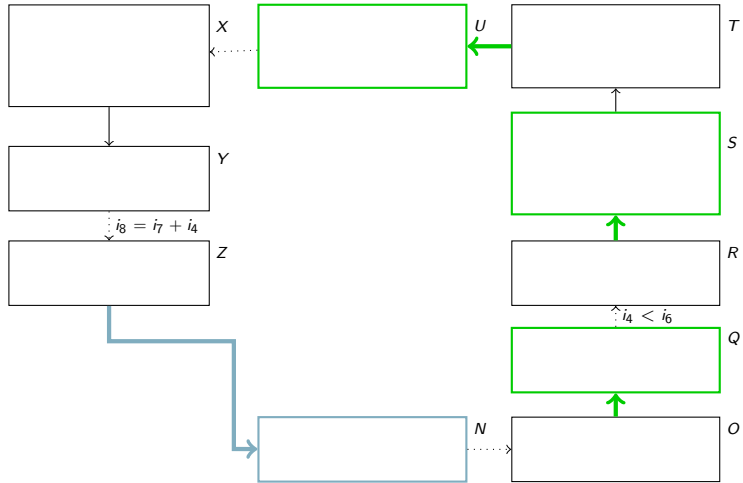
- 1 Introduction
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- Goal: Find state that is visited again and again

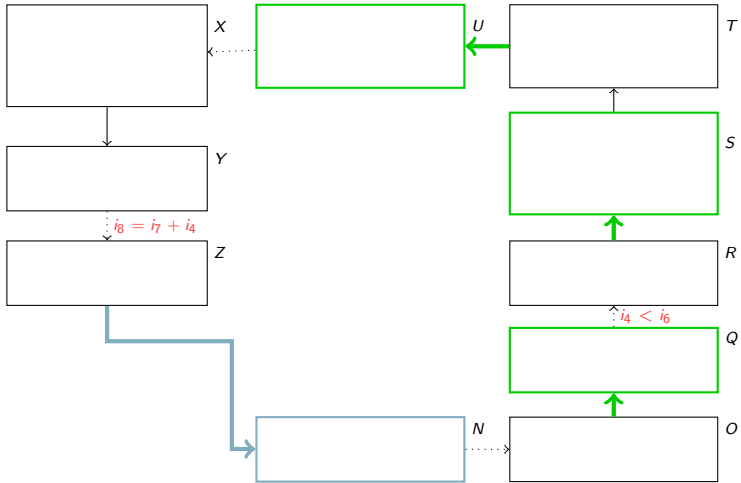


- Goal: Find state that is visited again and again
- ⇒ Only consider cycles
- Heuristic: Integers: Find values by SMT  
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- Goal: Find state that is visited again and again
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  - Objects: Find values by witness generation
- Verification: By symbolic evaluation

$$i_4 < i_6$$
$$\wedge i_8 = i_7 + i_4$$



Find values by SMT

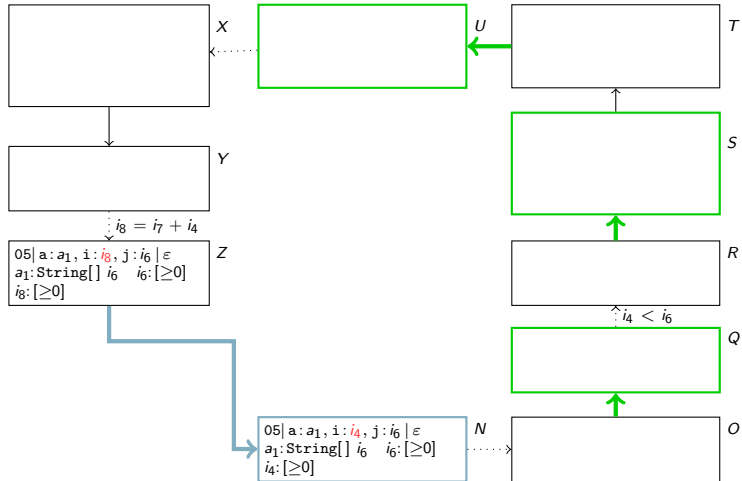
- Use conditions on edges



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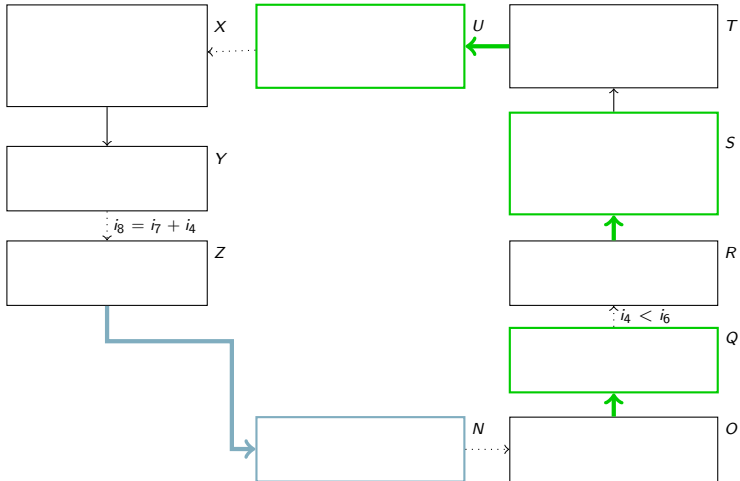
$$\wedge i_4 = i_8$$



## Find values by SMT

- Use conditions on edges
  - **Refinement**, **Instance** renamings  $\Rightarrow$  Equalities
- $\Rightarrow$  Last instance edge  $\sim$  values stay the same

$$\begin{aligned}
 & i_4 < i_6 \\
 \wedge & i_8 = i_7 + i_4 \\
 \wedge & i_4 = i_8
 \end{aligned}$$



Find values by SMT

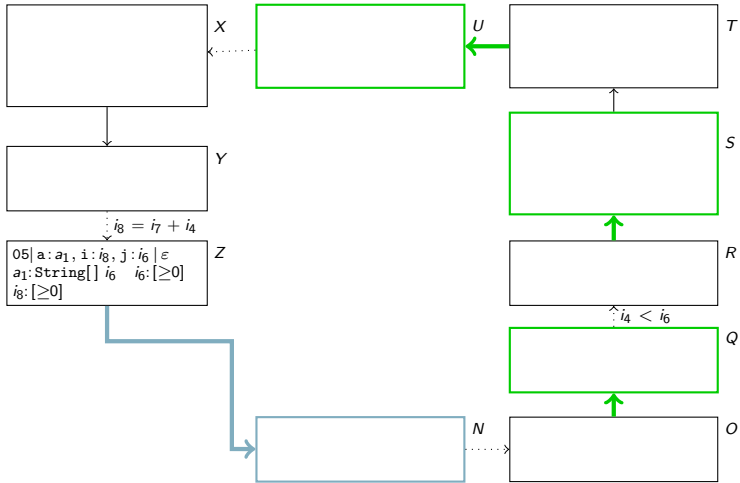
- Use conditions on edges
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SMT Solution:

$$\begin{aligned}
 i_4 &= i_7 = i_8 = 0 \\
 i_6 &= 1
 \end{aligned}$$

## Witness

```
05|a:a1, i:0, j:1|ε  
a1:String[] 1
```



Find values by witness generation

- Instantiate last loop state with integer solution

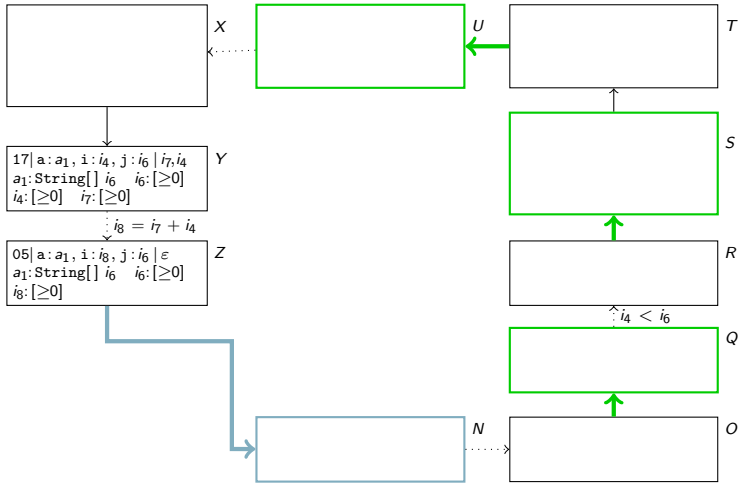
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```
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### Find values by witness generation

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- Perform witness generation

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```
05| a: a1, i: 0, j: 1 | ε  
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```
17| a: a1, i: 0, j: 1 | Q0  
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```
04| this: o5 | i7  
17| a: a1, i: i4, j: i6 | i4  
a1: String[] i6 i6: [≥0]  
o5: String(count = i7, ...) |  
i4: [≥0] i7: [≥0] a1 √ o5
```

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17| a: a1, i: i4, j: i6 | i7, i4  
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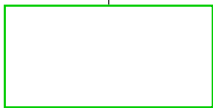
$$i_8 = i_7 + i_4$$



Z



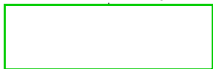
N



S



R



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O

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U



T

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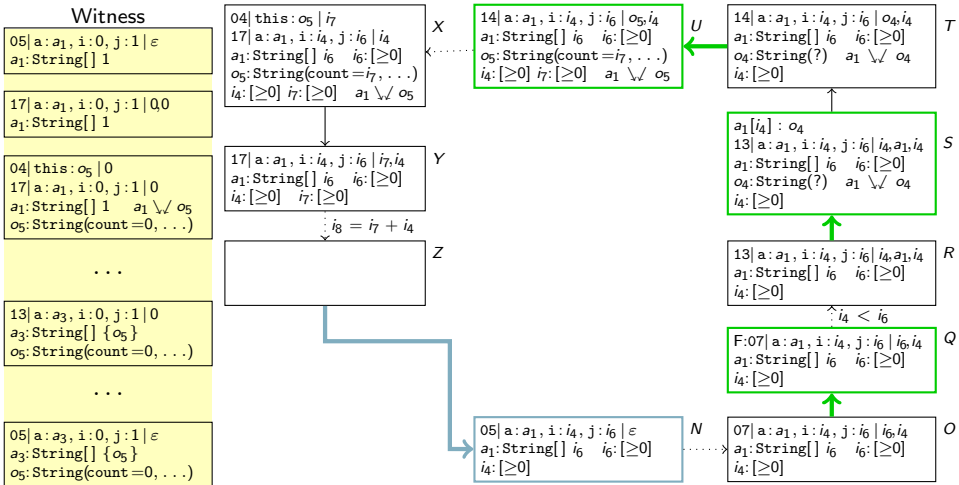
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## Find values by witness generation

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Already done:

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- Non-looping Non-termination
- Termination analysis

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Extensions:

- Use other SMT theories
- Use source code annotations
- ...

# Non-termination analysis of JBC

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  - 268 from the *Termination Problem Data Base*
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	Invel Ex.					Other Ex.				
	Y	N	F	T	R	Y	N	F	T	R
AProVE-No	1	51	0	3	5	204	30	12	24	11
AProVE	1	0	5	49	54	204	0	27	39	15
Julia	1	0	54	0	2	166	22	82	0	4
Invel	0	42	13	0	?					

**Y**es, **N**o, **F**ailed proof, **T**imeout, **R**untime (average)

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<http://aprove.informatik.rwth-aachen.de/eval/JBC-Nonterm>