

Functions Operating on the IO Monad

`putChar :: Char -> IO ()`

`getChar :: IO Char`

`(>>) :: IO a -> IO b -> IO b`

`return :: a -> IO a`

$$\boxed{\text{IO}_1} \text{ } \begin{array}{l} \text{a} \\ \swarrow \end{array} \text{ } >> \text{ } \boxed{\text{IO}_2} \text{ } \begin{array}{l} \text{b} \\ \swarrow \end{array} \text{ } = \text{ } \boxed{\text{IO}_1} \text{ } \boxed{\text{IO}_2} \text{ } \begin{array}{l} \text{b} \\ \swarrow \end{array}$$

`(>>=) :: IO a -> (a -> IO b) -> IO b`

$$\boxed{\text{IO}_1} \text{ } \begin{array}{l} \text{a} \\ \swarrow \end{array} \text{ } >>= \text{ } \begin{array}{c} \diagup \text{ } \diagdown \\ \boxed{\text{a}} \end{array} \text{ } \boxed{\text{IO}_2} \text{ } \begin{array}{l} \text{b} \\ \swarrow \end{array} \text{ } = \text{ } \boxed{\text{IO}_1} \text{ } \begin{array}{c} \diagup \text{ } \diagdown \\ \text{a} \end{array} \text{ } \boxed{\text{IO}_2} \text{ } \begin{array}{l} \text{b} \\ \swarrow \end{array}$$

`getChar >> return ()` reads a character and ignores it

`getChar >>= putChar` reads a character and prints it on the screen

do-Notation

```
gets :: Int -> IO String
gets 0      = return []
gets (n+1) = getChar >>= \x  ->
                           gets n  >>= \xs ->
                                         return (x:xs)
```

`p >>= \x ->` `do x <- p`
`q >>= \y ->` `y <- q`
 `r`

can be written as

```
gets :: Int -> IO String
gets 0      = return []
gets (n+1) = do x  <- getChar
                xs <- gets n
                return (x:xs)
```

Simple Evaluation Without Monads

```
data Value a = Result a
```

```
instance Show a => Show (Value a) where
    show (Result x) = "Result: " ++ show x
```

```
eval1 :: Term -> Value Float
eval1 (Con x)      = Result x
eval1 (Div t u)   = Result (x/y)
                    where Result x = eval1 t
                          Result y = eval1 u
```

Evaluation and Exceptions Without Monads

```
data Maybe a = Nothing | Just a
```

```
instance Show a => Show (Maybe a) where
    show Nothing    = "Nothing"
    show (Just x)   = "Just " ++ show x
```

```
eval2 :: Term -> Maybe Float
```

```
eval2 (Con x)    = Just x
```

```
eval2 (Div t u) = case eval2 t of
```

```
        Nothing -> Nothing
```

```
        Just x  -> case eval2 u of
```

```
            Nothing -> Nothing
```

```
            Just y  -> if y == 0
```

```
                then Nothing
```

```
                else Just (x/y)
```

Evaluation and Counting Without Monads

```
data ST a = MakeST (Int -> (a, Int))
```

```
apply :: ST a -> Int -> (a, Int)
```

```
apply (MakeST f) s = f s
```

```
instance Show a => Show (ST a) where
```

```
  show tr = "Result: " ++ show x ++ ", State: " ++ show s  
  where (x, s) = apply tr 0
```

```
eval3 :: Term -> ST Float
```

```
eval3 (Con x) = MakeST (\s -> (x, s))
```

```
eval3 (Div t u) = MakeST (\s -> let (x, s') = apply (eval3 t) s  
                           (y, s'') = apply (eval3 u) s'  
                           in (x/y, s''+1))
```

Simple Evaluation With Monads

```
data Value a = Result a
```

```
instance Show a => Show (Value a) where
    show (Result x) = "Result: " ++ show x
```

```
instance Monad Value where
    return          = Result
    Result x >>= q = q x
```

```
eval1 :: Term -> Value Float
eval1 (Con x)    = return x
eval1 (Div t u) = do x <- eval1 t
                     y <- eval1 u
                     return (x/y)
```

Evaluation and Exceptions With Monads

```
data Maybe a = Nothing | Just a
```

```
instance Show a => Show (Maybe a) where
    show Nothing     = "Nothing"
    show (Just x)   = "Just " ++ show x
```

```
instance Monad Maybe where
    return          = Just
    Nothing >>= q = Nothing
    Just x  >>= q = q x
```

```
eval2 :: Term -> Maybe Float
eval2 (Con x)      = return x
eval2 (Div t u)   = do x <- eval2 t
                        y <- eval2 u
                        if y /= 0 then return (x/y) else Nothing
```

Evaluation and Counting With Monads

```
data ST a = MakeST (Int -> (a, Int))    apply :: ST a -> Int -> (a, Int)
                                                    apply (MakeST f) s = f s
```

```
instance Show a => Show (ST a) where
  show tr = "Result: " ++ show x ++ ", State: " ++ show s
            where (x, s) = apply tr 0
```

```
instance Monad ST where
  return x = MakeST (\s -> (x, s))
  tr >>= q = MakeST (\s -> let (x, s') = apply tr s
                        in apply (q x) s')
```

```
eval3 :: Term -> ST Float
eval3 (Con x) = return x
eval3 (Div t u) = do x <- eval3 t
                      y <- eval3 u
                      increase
                      return (x/y)
```

```
increase :: ST ()
increase = MakeST (\s -> ((), s+1))
```