$$\mathcal{R}_0: f(x, f(y, z)) \rightarrow f(f(x, y), z)$$
 (G1)
 $f(x, e) \rightarrow x$ (G2)
 $f(x, i(x)) \rightarrow e$ (G3)

r:
$$\underbrace{(G1)}_{(G1)} \mathsf{f}(x,\mathsf{f}(y,\mathsf{i}(y))) \underbrace{(G3)}_{(G3)}$$

$$\mathsf{f}(x,\mathsf{e})$$

$$\mathcal{R}_1: \mathcal{R}_0 \cup \{(G4)\}$$
 with $f(f(x,y), i(y)) \rightarrow x \quad (G4)$

Success: $\mathcal{R}_0, \mathcal{R}_1, \dots, \mathcal{R}_n$

and all $\langle s, t \rangle \in CP(\mathcal{R}_n)$ are joinable

Failure: $\mathcal{R}_0, \mathcal{R}_1, \dots, \mathcal{R}_n \text{ and } \langle s, t \rangle \in CP(\mathcal{R}_n)$

with normal forms s', t' where $s' \neq t'$, $s' \not\succ t'$, $t' \not\succ s'$.

Non-Termination: $\mathcal{R}_0, \mathcal{R}_1, \ldots$ terminating, equivalent, not confluent